
Efficiency analysis of German electricity distribution utilities – non-parametric and parametric tests

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This study applies non-parametric and parametric tests to assess the efficiency of electricity distribution companies in Germany. Traditional issues in electricity sector benchmarking are addressed, such as the role of scale effects and optimal utility size, as well as new evidence specific to the situation in Germany. Labour, capital, and peak load capacity are used as inputs, and units sold and the number of customers as output. The data cover 307 (out of 553) German electricity distribution utilities. A data envelopment analysis (DEA) is applied with constant returns to scale (CRS) as the main productivity analysis technique, whereas stochastic frontier analysis (SFA) with distance function is the verification method. The results suggest that returns to scale play but a minor role; only very small utilities have a significant cost advantage. Low customer density is found to affect the efficiency score significantly, in particular in the lower third of all observations. Surprisingly, East German utilities feature a higher average efficiency than their West German counterparts. The correlation tests imply a high coherence of the results.

I. Introduction

Efficiency analysis has played a crucial role in defining regulatory policies, mainly in industries characterized by natural monopolies and/or by public ownership. Examples are telecommunication (e.g. Uri, 2001), transport (Coelli and Perelman, 1998, 2000), energy (e.g. Jamasb and Pollitt, 2001, 2003), schooling (e.g. Mizala *et al.*, 2002), hospitals (e.g. Steinmann and Zweifel, 2003) and even museums (e.g. Bishop and Brand (2003) using a stochastic analysis of museums in South Western England).

Efficiency analysis is also increasingly applied for other sector-specific analysis, such as farming (e.g. Latruffe *et al.*, 2004, on crop and livestock farms), banking (e.g. Färe *et al.*, 2004; Hauner, 2005), or the cement industry (Tsekouras and Skuras, 2005). In the electricity sector, efficiency analysis has played a particularly important role in the liberalization process towards a competitive industry structure and market-orientated regulation, both in electricity transmission and electricity distribution. The objective of this study is to assess the relative efficiency of decision-making units (here: electricity distribution

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companies), in order to generate information for an incentive-oriented regulation, with benchmarking and yardstick competition.

Data envelopment analysis (DEA) and stochastic frontier analysis (SFA) are the most commonly used methods in the literature on benchmarking and efficiency analysis in the electricity sector. They have been particularly useful in the regulatory process in Great Britain, Switzerland, the Nordic States, the Netherlands and Austria. Many authors concentrate on scale effects, and the optimal size and relative efficiency of utilities. Jamasb and Pollitt (2001) give an extensive comparison of international efficiency studies for the electricity sector, stressing the importance of the proper variable choice. In a subsequent paper, Jamasb and Pollitt (2003) perform an international benchmarking study of 63 utilities from six European countries comparing several SFA and DEA specifications. Although they determine a high correlation among the models, the results for single utilities differ noticeably. Using panel data of 59 Swiss distribution companies over eight years, Farsi and Filippini (2004) argue that different methodologies may lead to different results, but that the reasonable out-of-sample ‘prediction errors suggest that panel data models can be used as a prediction instrument in order to narrow the information gap between the regulator and regulated companies’ (p. 2). In a similar panel data analysis for six Latin America countries, Estache *et al.* (2004) also show that national regulators can reduce information asymmetry through cross-country efficiency analysis.

Other examples of panel-data approaches are Burns *et al.* (1999) with a dynamic benchmarking analysis for 12 regional electricity distribution utilities in Great Britain, Hjalmarsson’s (1992) analysis of Swedish electricity retail distributors, and the productivity study of Norwegian electricity utilities conducted by Førsund and Kittelsen (1998). Quality is recently explicitly taken into account and related to benchmarking in a study by Giannakis *et al.* (2004) on the UK electricity distribution utilities.

The present study is the first productivity analysis of German electricity distributors to date. Both traditional issues of electricity sector benchmarking are addressed, such as the role of scale effects and optimal utility size, as well as new evidence specific to the situation in Germany. Regarding the latter, the potential effects of three structural variables are considered: consumer density, grid composition (cable versus aerial lines), and differences between

East and West German distribution companies. The empirical section thus follows the structural criteria set out by the German association agreements (*‘Verbändevereinbarung Strom VV II+’*), a predecessor of the new energy law of 2005. The data cover 307 (out of 553) German electricity distribution utilities.¹

Our study is motivated by two factors: first, efficiency analysis in electricity distribution currently faces serious issues in determining whether there are significant returns to scale. The question arises whether or not smaller utilities do have systematically lower efficiency scores than larger ones, implying increasing returns (‘big is beautiful’). Filippini (1998), Filippini *et al.* (2004), and a number of other studies suggest significant economies of scale in ‘small’ electricity distribution systems, e.g. Switzerland and Slovenia. Smaller utilities could reduce costs by merging and thereby extending their sub-optimal service territory size. This would suggest that the current, atomized structure of the German electricity utilities may be subject to structural change as well. Second, in the wake of liberalization, the German electricity industry is currently undergoing structural change from local monopolies to regulated competition. Observers suggest that liberalization will lead to a structural change of the sector, which has up to now comprised a large number of companies: four in high-voltage transmission, 56 in regional distribution, and 553 in local electricity distribution. These numbers contrast sharply with the UK system, for instance, which features only 13 regional electricity companies altogether.

The next section briefly describes the institutional context of electricity sector reform in Germany. Section III presents our methodology and data. Results from the basic model, and from several extended models, estimated by using DEA and SFA are provided in Section IV; a correlation analysis of different estimations is also carried out. Section V concludes.

II. Electricity Sector Reforms in Germany

Germany is the largest electricity producer and consumer in the European Union, and thus plays an important role in the liberalization of the sector launched by the European Commission in the mid-1990s. However, until recently, Germany has held the red lantern of the countries resisting European electricity deregulation, together with France and a

¹ In a previous (discussion paper) version of this study, a sample of 380 utilities is used. The reduction of the sample size was due to the inclusion of the inverse density index, and the exclusion of evident outliers with doubtful data.

few other countries. Subsequently the European Union has speeded up its attempts towards liberalization and vertical unbundling of the electricity sector. The so-called 'acceleration directive' (2003/54/EC) requires legal unbundling of electricity distribution companies with more than 100 000 connected customers, i.e. creating legally independent commercial units for generation, transmission and distribution. This goes well beyond the former EU electricity directive 96/92. Given the slow progress of liberalization in most member states, the acceleration directive also calls for an intensification of regulatory oversight and the introduction of an explicit regulatory body in each country, responsible for regulating electricity distribution. A review of the implementation of the acceleration directive is scheduled for 2007.

Consequently, in Germany the electricity industry will now be subordinated to ex-ante regulation for the first time in its history. Under the former directive 96/92, Germany had implemented a model of negotiated access and had – to that end – authorized industry self-regulation. The electricity industry and the large electricity consumers were given freedom to negotiate network access prices and conditions in so-called association agreements ('Verbänderevereinbarungen'). Given the systematic information advantage of the electricity industry over the customers, and the hesitation of the German government to establish a sufficient countervailing power in a regulatory agency, self-regulation did not succeed in bringing prices down, or in establishing a significant level of competition. In its annual benchmarking reports, the European Commission has regularly criticized the German approach of self-regulation of network access charges (e.g. European Commission, 2003).² The new German energy law, in force since July 2005, therefore set up a regulatory agency and required ex-ante regulation of network access. As observed in other countries implementing UK-style reforms, e.g. the Netherlands and Austria, the process of unbundling and the introduction of ex-ante regulation are likely to lead to conflicts between the incumbent operators, potential market entrants and the regulatory authorities. These conflicts revolve around the absolute level of access tariffs, the relative level, and non-tariff discrimination.

Surprisingly, the literature on that issue in Germany is sparse: Riechmann (2000) investigates the efficiency of the 53 regional distributors in Germany with DEA and finds significant cost

reduction potentials. Haupt *et al.* (2002) compare network access prices of German electricity distributors and identify reasons for differences beyond the decision framework of the companies. They consider structural variables in order to take explicit account of regional specificities, for example settlement density and consumer structure; but they do not include a comparative efficiency analysis. Growitsch and Wein (2005) try to explain the high network charges in German electricity distribution, but efficiency considerations are not included in the analysis. In a study for the German energy consuming industry, Frontier Economics and Consentec (2003) assess a sample of 27 regional and local electricity distributors, using turnover as input, and peak load, units sold, and structural parameters as output. Interestingly, a regional distributor in East Germany was found to be on the efficient frontier, indicating that the traditional post-reunification bias towards higher costs in East German distribution may have decreased by now.

III. Methodology and Data

Methodology

To measure the relative efficiency of the German distribution utilities the traditional data envelopment analysis (DEA) is used as well as stochastic frontier analysis (SFA), including the multi-output multi-input version of the distance function, mainly as a verification method. The analysis is confined to the measurement of technical efficiency. DEA is a non-parametric approach determining a piecewise linear efficiency frontier along the most efficient utilities to derive relative efficiency measures of all other utilities. The efficiency scores can be obtained either within a constant returns to scale (CRS) approach or a less restrictive variable returns to scale (VRS) approach. The VRS approach compares companies only within similar sample sizes; this approach is appropriate if the utilities are not free to choose or adapt their size. Therefore it is argued that the CRS approach is more relevant for the analysis. It assumes that companies are flexible to adjust their size to the one optimal firm size at least in the German context. However, the VRS model is also calculated in order to report scale efficiency information, which is delivered by the difference between the CRS and VRS scores.

² See Brunekreeft (2003), Brunekreeft and Tweleemann (2005) for a detailed account of the regulatory context in German electricity.

The determination of the efficiency score of the i -th firm in a sample of N firms in the CRS model is equivalent to the following optimization:

$$\begin{aligned} & \min_{\theta, \lambda} \theta \\ & \text{s.t.} \\ & -y_i + Y\lambda \geq 0 \\ & \theta x_i - X\lambda \geq 0 \\ & \lambda \geq 0 \end{aligned}$$

θ is the efficiency score, and λ a $N \times 1$ vector of constants. Assuming that the firms use E inputs and M outputs, X and Y represent $E \times N$ input and $M \times N$ output matrices, respectively. The input and output column vectors for the i -th firm are represented by x_i and y_i . The constraints ensure that the i -th firm is compared with a linear combination of firms similar in size. To determine efficiency measures under the VRS assumption a further convexity constraint $\sum \lambda = 1$ has to be considered. The system is solved once for each firm (for details, see Jamasb and Pollitt, 2003, 1612; Coelli *et al.*, 1998, Chapter 6).

Calculations can be done using an input-orientation or an output-orientation. The input-orientation considers the output to be fixed so that the input has to be adjusted in order to maximize efficiency. In the output-orientation, inputs are considered fixed and the objective is the maximization of output. Traditionally, efficiency analyses in the electricity sector assume the output fixed in a market with the legal duty to serve all customers in a predefined service territory. In order to avoid potential errors of misspecification, both input- and output efficiency measures are calculated. The two measures provide the same value under CRS and estimate exactly the same frontier, therefore identify the same set of utilities being on the efficient frontier; (see Coelli, 1998). The VRS results obtained under the output-orientated approach do not differ significantly in comparison with the input-orientation.

DEA is a relatively uncomplicated approach. The determination of an explicit production function is not required. However, since DEA is a non-parametric approach the impact of the respective input factors on the efficiency cannot be determined. Furthermore, DEA does not account for possible noise in the data and outliers can have a large effect on the result. Therefore a second methodology is introduced, the stochastic frontier analysis (SFA). SFA delivers a parametric approach to efficiency benchmarking. The theory of stochastic frontier

production functions was originally proposed by Aigner *et al.* (1977) as well as Meeusen and van den Broeck (1977). This approach requires the definition of an explicit production or cost function. Based on the usual OLS regression a parallel shift of the original production function yields the efficiency frontier. This is caused by an underlying assumption splitting the error term into a stochastic residuum (noise) and an inefficiency-term. Usually, stochastic errors are assumed to be distributed half-normally. Originally the model was specified for cross-sectional data. Hence, the mathematical expression of the production process is:

$$Y_i = x_i\beta + (v_i - u_i) \quad i = 1, \dots, N \quad (1)$$

where Y_i is output (or the logarithm of output) of the i -th firm,

x_i is a $k \times 1$ vector of input quantities of the i -th firm,

β is a vector of parameters to be estimated, v_i are random variables which are assumed to be i.i.d. $N(0, \sigma_v^2)$, independent of u_i .

u_i are non-negative random variables usually assumed to be half normal distributed (i.i.d. $|N(0, \sigma_u^2)|$), thereby accounting for individual technical inefficiency.

This original specification has been extended by different assumptions on the distribution of u_i , such as truncated normal or two-parameter gamma distributions. The further extension of the model to panel data, systems of equations and time-varying technical efficiencies follows more recent developments in econometrics and productivity analysis.

SFA is more complex than DEA in terms of data requirements and handling, but has the advantage of allowing one to deal with multiple-inputs³ in the form of a distance function, originally proposed by Shephard (1970). The basic idea is that in the case of a given production possibility frontier, for every producer the distance from the production frontier is a function of the vector of inputs used, X , and the level of outputs produced, Y . For the output-oriented model the distance function is defined as:

$$D_o(X, Y) = \min \left\{ \theta : \left(\frac{Y}{\theta} \right) \in P(x) \right\} \quad (2)$$

where $D_o(X, Y)$ is the distance from the firm's output $P(X)$ set to the production frontier. $D_o(X, Y)$ is non-decreasing, positively linearly homogeneous and convex in Y , and decreasing in X . θ is the scalar

³ See Coelli and Perelman (2000). They measure the technical efficiency of European railways by means of a distance function approach and illustrate its usefulness in the analysis of production in multi-output industries.

distance by which the output vector can be deflated (Coelli, 2002) and can be interpreted as the level of efficiency. The output distance function aims at identifying the largest proportional increase in the observed output vector Y provided that the expanded vector (Y/θ) is still an element of the original output set (Grosskopf *et al.*, 1995). If Y is located on the outer boundary of the production possibility set then $D_o(X, Y) = \theta = 1$ and the utility is 100% efficient. On the other hand, values of $D_o(X, Y) = \theta \leq 1$ indicate inefficient enterprises lying within the efficiency frontier.

The input orientated approach is defined on the input set $L(Y)$ and considers, by holding the output vector fixed how much the input vector may be proportionally contracted. The input distance function is expressed by:

$$D_i(X, Y) = \max \left\{ \rho: \left(\frac{X}{\rho} \right) \in L(Y) \right\} \quad (3)$$

$D_i(X, Y)$ is non-decreasing, positively linearly homogeneous and concave in X , and increasing in Y . ρ is the scalar distance by which the input vector can be deflated. If $D_i(X, Y) = \rho = 1$, X is located on the inner boundary of the input set and the utility is 100% efficient.

The first step is to estimate the distance from the frontier. Therefore both the efficiency frontier as well as the relationship between inputs and outputs has to be determined. These considerations also include the case of multi-output production functions which cannot be estimated with conventional SFA techniques. The most common and appropriated functional form is the translog production function. The translog input distance function in its parametric form with $M(m = 1, 2, \dots, M)$ outputs and $K(k = 1, 2, \dots, K)$ inputs is specified as (Coelli, 2002)

$$\begin{aligned} \ln(D_i) = & \alpha_0 + \sum_{m=1}^M \gamma_m \ln y_m + \frac{1}{2} \sum_{m=1}^M \sum_{n=1}^M \gamma_{mn} \ln y_m \ln y_n \\ & + \sum_{k=1}^K \beta_k \ln x_k + \frac{1}{2} \sum_{k=1}^K \sum_{l=1}^K \beta_{kl} \ln x_k \ln x_l \\ & + \sum_{k=1}^K \sum_{m=1}^M \delta_{km} \ln x_k \ln y_m \end{aligned} \quad (4)$$

In order to maintain the homogeneity and symmetry a number of restrictions need to be imposed. For homogeneity the following restrictions have to be considered:

$$\sum_{k=1}^K \beta_k = 1, \sum_{l=1}^K \beta_{kl} = 0 \text{ and } \sum_{k=1}^K \delta_{km} = 0 \quad (5)$$

For symmetry, two other restrictions have to be observed:

$$\gamma_{mn} = \gamma_{nm} \text{ and } \beta_{kl} = \beta_{lk} \quad (6)$$

Imposing homogeneity and symmetry restrictions and normalizing Equation 4 by dividing it by one of the inputs delivers the estimating form of the input distance function:

$$\begin{aligned} -\ln(x_K) = & \alpha_0 + \sum_{m=1}^M \gamma_m \ln y_m \\ & + \frac{1}{2} \sum_{m=1}^M \sum_{n=1}^M \gamma_{mn} \ln y_m \ln y_n + \sum_{k=1}^{K-1} \beta_k \ln \left(\frac{x_k}{x_K} \right) \\ & + \frac{1}{2} \sum_{k=1}^{K-1} \sum_{l=1}^{K-1} \beta_{kl} \ln \left(\frac{x_k}{x_K} \right) \ln \left(\frac{x_l}{x_K} \right) \\ & + \sum_{k=1}^{K-1} \sum_{m=1}^M \beta_{km} \ln \left(\frac{x_k}{x_K} \right) \ln y_m - \ln D_i \end{aligned} \quad (7)$$

$\ln D_i$ can be interpreted as error term which reflects the difference between the observed data realizations and the predicted points of the estimated function. Replacing $\ln D_i$ by a composed error term (the stochastic error v_i and the technical inefficiency u_i) yields the common SFA form. It can be estimated by a stochastic frontier production function defined as $y = f(x) + v - u$. For $I(i = 1, \dots, I)$ firms, this econometric specification with $\ln D_{0i} = v_i - u_i$, in its normalized form is expressed by:

$$\begin{aligned} -\ln(x_{Ki}) = & \alpha_0 + \sum_{m=1}^M \gamma_m \ln y_{mi} \\ & + \frac{1}{2} \sum_{m=1}^M \sum_{n=1}^M \gamma_{mn} \ln y_{mi} \ln y_{ni} \\ & + \sum_{k=1}^{K-1} \beta_k \ln \left(\frac{x_{ki}}{x_{Ki}} \right) \\ & + \frac{1}{2} \sum_{k=1}^{K-1} \sum_{l=1}^{K-1} \beta_{kl} \ln \left(\frac{x_{ki}}{x_{Ki}} \right) \ln \left(\frac{x_{li}}{x_{Ki}} \right) \\ & + \sum_{k=1}^{K-1} \sum_{m=1}^M \beta_{km} \ln \left(\frac{x_{ki}}{x_{Ki}} \right) \ln y_{mi} + v_i - u_i \end{aligned} \quad (8)$$

As discussed above, a certain distribution for u_i has to be assumed in order to separate stochastic and inefficiency effects.

Choice of variables and data

In the literature, a variety of specifications is employed depending on what exactly is being investigated and which variables are being used as inputs and as outputs.⁴ The choice of variables for input and output needs to take into account the international experience with electricity distribution benchmarking, and is constrained by data availability. In this respect, Germany has to be ranked among the least developing countries. The absence of regulation has thus far prevented the systematic collection of the relevant data. One therefore has to cope with a data set providing a representative sample for one year only (2001).

A base model is estimated, using the traditional input and output variables, and then variations are added to this model. The base models include labour, grid size and peak load (as the proxy for transformation capacity) as inputs, and units sold, the number of customers and the inverse density index as outputs. In the extended models, one disaggregates both the consumers (number of industrial and number of residential customers) and the type of cable (aerial and underground), and an additional input variable is introduced: the electricity losses by each company. Last but not least, the performance of utilities in East Germany and in West Germany are compared to check whether this historical distinction still causes a structural difference between the two regions. The data specification is as follows:

- Labour input is estimated by the number of workers.⁵ Some of the utilities have their own generating plants and only employment data covering all workers in the electricity utility is disposed of. To get an approximation of workers employed in electricity distribution, one employee is subtracted for each 20 GWh electricity produced (following Auer, 2002, p. 128).

- Capital input is approximated by the length of the existing electricity cables. Voltage levels (high, medium and low voltage) are differentiated between by introducing a cost factor for each type of line.⁶ In addition, in one of the extended models, the study distinguishes between the cable grid and the aerial grid (following Auer, 2002, and others); cable is supposed to be more expensive than aerial grid. Thus, the simple grid size variable of the basic model is substituted by a weighted sum of cable and aerial grid.⁷
- One model also takes into account the maximum peak load as a further cost factor to approximate transformer capacity.
- The amount of electricity distributed to end users (units sold) and the total number of customers are used as output variables; in an extended model turnover (national revenue) is used instead of units sold as a further output variable.⁸
- Losses are included as a proxy for the technical quality of the grid or the service quality of the grid. Losses are considered as an input.⁹
- The use of the inverse density index (settled area in square kilometres per inhabitant) in the base model specification is motivated by the argument that utilities with a dense customer structure have a natural cost advantage over those with a weak customer density. When taken as an output, the inverse density index improves the performance of sparsely inhabited distribution areas.¹⁰
- In addition, utilities situated in West Germany are distinguished between those in East Germany (the former GDR). The latter are expected to display particularities due to their socialist heritage which may have a significant effect on their efficiency scores. An example is increasing costs because of the rough surface a utility has to cope with; another one is the density of a territory that a utility has to serve.

⁴ For example, most studies consider the grid size as an input to approximate the capital costs whereas other studies cited by Jamasb and Pollitt (2001) specify the total length of line as output variable to approximate the complexity of the grid structure. Likewise, the transformer capacity is found to be an input in 11 of the 20 studies analysed, whereas two of the studies chose it as an output.

⁵ One is aware of the criticism of this choice of variable due to the potentially distorting effect of outsourcing: a utility can improve its efficiency simply by switching from in-house production to outsourcing.

⁶ Following standard practice used by the German network association (VDN): factor 5 for high voltage, 1.6 for medium voltage, and 1 for low voltage cables.

⁷ The share of cable lines of total lines is one of the structural variables in the German association agreements.

⁸ Due to data limitations, one cannot differentiate between operating costs (OPEX) and capital costs (CAPEX). For curiosity reasons, a model specification has also been run using turnover as the only input. If one assumes identical profitability among the distribution companies, then turnover can be used as a proxy for total costs (TOTEX).

⁹ Alternatively, other studies use the inverse of the losses as an output.

¹⁰ Density is also one of the structural variables defined in the German association agreements.

Table 1. Sample summary statistics

Variable	Obs.	Mean	Std. dev.	Min	Max
Units sold (MWh)	307	346 306.3	1 182 148	5675	1 420 000 000
No. of customers	307	38 494.9	103 225.8	7	1 060 000
Grid size (km)	307	1190.7	3328.4	20.60	38 899
Labour	307	100.6	291.1	2	3077
Inv. density index	307	0.0027	0.0034	0.00022	0.028
Peak load (kW)	195	78 265.6	2 191 046	1363	2 041 000
Turnover (mn.EUR)	195	49 595.1	1 806 072	597	2 182 300
Losses (MWh)	195	21 690.9	1 065 133	53	1 340 262
Aerial line (km)	195	213.5	5807	1	5529
Cable line (km)	195	1189.9	26 047	12.4	192 234
Non res. customers	195	45 197.8	1 118 686	60	909 000
Res. customers	195	4639.5	137 061	2	151 000

Also, electricity consumption has plummeted significantly since the end of socialism, and the existing networks may have been too extensive.

The electricity distribution data used in this study include information on 307 German distribution companies in the year 2001 (or, for some variables, previous years). The data were collected from publicly available sources.¹¹ It has been verified that the sample is representative: it covers 56% of the total number of utilities, and 60.3% of the electricity sold. For the models 3–7, there are 197 observations. Summary statistics of the data are presented in Table 1.

IV. Empirical Results

Overview of the model runs

The presentation of results is divided into two broad sections: in the first section, the base model is developed, consisting of two inputs (labour, network size) and three outputs (units sold, number of customers, inverse density index). Subsequently, variations were run on the base model, including the use of turnover as a monetary variable (instead of units sold), a disaggregation of the

consumers (industrial and residential), as well as a disaggregation of the network (into aerial lines and underground cable). Further, peak load is considered as a proxy for transformer capacity (for which no data are available). To extend the classical efficiency measurement approach quality is included: grid quality is approximated by the sum of losses as a further input variable. Results for East and West Germany will also be discussed separately. Models 1 and 2 are separately estimated with DEA (CRS and VRS) and SFA,¹² and the correlations and rank-correlations are checked. Models 3–7 are limited to DEA. The limited data availability for firm-specific characteristics leads to a reduced data sample of 195 utilities in the second approach. Since Model 2 is estimated with the full data sample as well as with the reduced data sample, it serves as reference model to compare results obtained in the two parts. Table 2 lists the different model specifications in more detail.

Results from the base model

Model 1. Model 1 considers two inputs (labour and grid size) and two outputs (units sold and number of customers). DEA delivers the efficiency estimates depicted in Fig. 1.¹³ The average efficiency for Model 1 is 63.2%. Twelve utilities are on the efficient frontier. A positive correlation is observed between the size of the utility and its efficiency score: the

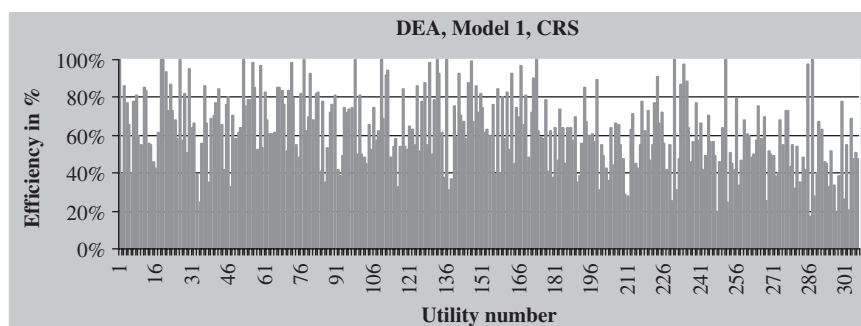
¹¹ The sources of the data are the following: Verlags-und Wirtschaftsgesellschaft der Elektrizitätswerke m.b.H. – VWEW; ‘Jahresdaten der Stromversorger 2001’; VWEW Energieverlag GmbH, Frankfurt am Main, Heidelberg (2002) for number of customers, units sold, number of employees and grid data; VDEW-Statistik 1996/1997 Leistung und Arbeit; VWEW-Verlag, Frankfurt am Main; (1997/98) for inverse density index and peak load. Some data were also discovered by internet research on the utilities’ homepages.

¹² DEA was conducted using the Computer program DEAP Version 2.1; for SFA, the software package FRONTIER Version 4.1 was used. Both were written by T. Coelli.

¹³ In Fig. 1 as well as in all subsequent figures, the utilities are ordered by units sold and, thereby, by size. Thus, utility No. 1 is the largest in size, and utility No. 307 the smallest.

Table 2. Model specification for the analysis

	Labour	Grid size	Losses	Peak load	Units sold	Turnover	No. of customers	Inverse density I
Model 1	I	I			O		O	
Model 2	I	I			O		O	O
Model 2, VRS	I	I			O		O	O
Model 2, West/East	I	I			O		O	O
Model 3	I	I		I	O		O	O
Model 2b	I	I					O	O
Model 4	I	I				O	O	O
Model 5	I	I	I		O		O	O
Model 6, Grid disaggregated	I	I			O		O	O
Model 7, Cust. disaggregated	I	I			O		O	O



Average efficiency: 63.20%.

307 utilities.

Input: labour, grid size.

Output: customers, units sold.

Fig. 1. DEA Analysis, Model 1 with CRS

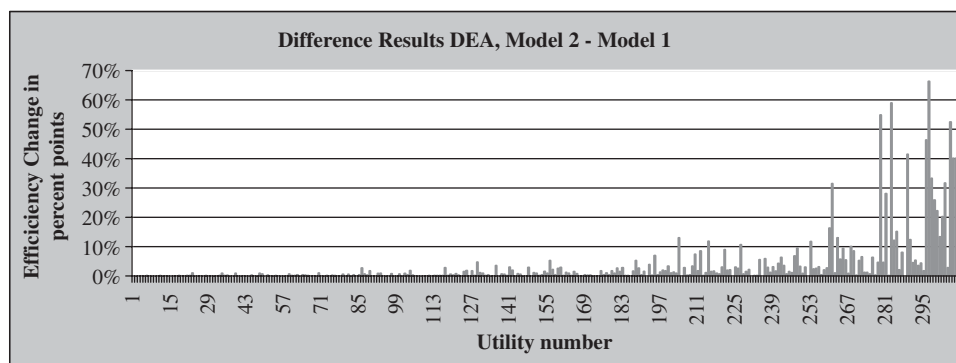
average efficiency for the 154 largest utilities is 69%, whereas for the smaller half of the sample it is only 57%. In particular, there seems to be a problem with very small utilities: the 25 smallest distribution companies average an efficiency score of only 41.4%.

If one uses the VRS specification of Model 1 instead, the efficiency scores rise significantly: 32 of the 307 utilities are on the efficient frontier. This can be explained by the fact that now utilities of similar size are compared with each other and not with the best ones in the sample. With VRS, the average efficiency increases to 68.3%, 5.1% higher than the results under the CRS assumption. For individual utilities, this improvement is significantly higher, in particular for the smaller ones. However, the largest companies are also considered more efficient under the VRS assumption because they are operating in an area of decreasing returns to scale. This may imply that they are too big to be efficient. Further analyses

and specifications will show that some of the inefficiencies detected in the base model can be explained by further firm-specific characteristics or structural variables.

Impact of structural particularities. The following analysis addresses the first two structural variables that are used in the association agreement's assessment of potential cost drivers: density, and East-West structure. It is reasonable to assume that regional particularities can have a strong impact on the efficiency of distribution utilities, although they are outside their decision framework. As mentioned before an example is increasing costs because of the rough surface a utility has to cope with; another one is the density of a territory that a utility has to serve.

Model 2 measures the first structural variable, the inverse density index, defined as service territory in kilometres divided by the number of



307 utilities.

Input: labour, grid size.

Output: customers, units sold, inverse density index (model 2)

Fig. 2. Differences for each utility between measures of Model 2 and Model 1

inhabitants of the region.¹⁴ This structural variable increases the efficiency of utilities in sparsely settled regions.¹⁵

The average productivity for model 2 increases moderately compared with Model 1, from 63.2% to 66.7%. Fifteen utilities are on the efficient frontier, three more than under the CRS assumption for Model 1. Figure 2 compares the CRS result for Model 2, including the inverse density index, with the CRS result from Model 1 (without structural variable). It turns out that for the 190 largest utilities, the structural effect is less significant (average efficiency increase of 0.4%), whereas for the smaller ones, density is an important cost driver (average increase of 6.9%); the effect is particularly strong for the 50 smallest utilities,¹⁶ because considered relatively: density, as a cost driver, has a higher impact for smaller utilities.

If we use the VRS specification of model 2 instead, the efficiency scores rise significantly. 35 of the 307 utilities are on the efficient frontier, which can again be explained by the fact that now utilities of similar size are compared with each other, and not with the best ones in the sample. With VRS, the average efficiency increases to 69.9%, 3.2% higher than the

results under the CRS assumption. For individual utilities, this improvement is significantly higher, in particular for the smallest but also the largest ones. Figure 3 shows the difference in efficiency scores between the VRS and the CRS model. It seems that the optimal utility size, i.e. the one where the VRS and the CRS efficiency scores converge, is around utility number 100 in the sample. This corresponds to about 200 GWh sold. Figure 3 also makes one issue clear: on the one hand smaller utilities could significantly gain in efficiency by merging; in this area, considerable economies of scale can be realized. On the other hand also larger utilities could become more efficient by becoming smaller.¹⁷

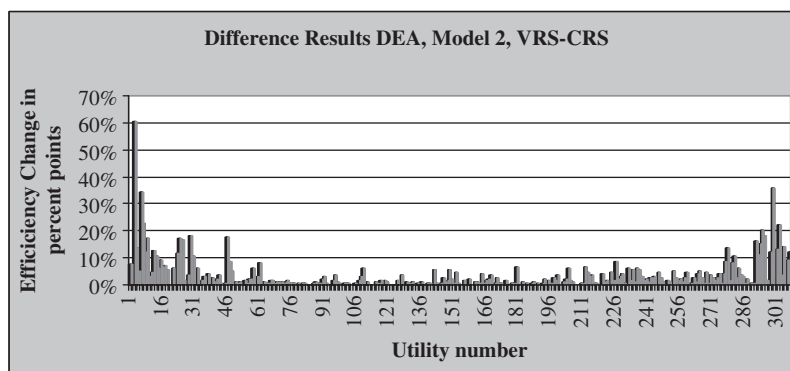
Correlation analysis and verification with SFA. Before continuing the DEA estimations of the extended models the robustness of the results are checked with a stochastic frontier analysis (SFA), the input distance approach. The correlation analysis of the results serves as verification of the obtained DEA efficiency measures. For verification with SFA a translog input distance function specification is used. In fact, this is a curved productivity function, similar to DEA-VRS where economies of scales are not

¹⁴ The inverse density index may also pick up some of the topographical particularities, since regions with a rough topography tend to have a lower density.

¹⁵ DEA considers this effect under the present specification as an increase in output that will increase the estimated efficiency of utilities in sparsely settled areas. Companies with a higher inverse density index and thereby a territory with few customers per square kilometre will increase their efficiency.

¹⁶ The extreme case is utility no. 297, which increases its efficiency score by 66.3 percentage points.

¹⁷ The nature of the scale inefficiencies (due to increasing or decreasing returns to scale) can directly be determined in DEAP Version 2.1 by running an additional DEA problem with non-increasing returns to scale (NIRS) imposed; (for more details see Coelli, 1998, p. 151). The empirical results indicate that large utilities are operating in an area of decreasing returns to scale, whereas the smaller utilities of the sample are operating in an area of increasing returns to scale. However, to make a definitive statement about the optimal utility size for the German electricity distribution sector, a more detailed analysis would be required.



307 utilities.

Input: labour, grid size.

Output: customers, units sold, inverse density index.

Fig. 3. Difference results DEA, Model 2, VRS-CRS

Table 3. Correlation analysis for Models 1 to 2, sample size 307

Sample utilities	DEA – VRS Model 1	DEA – VRS Model 2	SFA – DF Model 1	SFA – DF Model 2
DEA – VRS Model 1	1.00	0.97	0.81	0.74
DEA – VRS Model 2		1.00	0.77	0.76
SFA – DF Model 1			1.00	0.89
SFA – DF Model 2				1.00

considered to be relevant for efficiency. Therefore, it is more appropriate to compare the SFA results with DEA VRS.

Table 3 presents the correlation between the DEA and the SFA approaches for the first two models. All correlations are above 75% and thus seem to be significant. It can be concluded that the obtained DEA measures can generally be assumed to be robust and coherent. For the following analyses, the (stricter) constant returns to scale approach is applied to the sample. This implies that the size of companies is flexible. Given the recent liberalization of the sector, and the fact that mergers do occur regularly, this seems to be the more realistic assumption.

Analysis of differences between East and West Germany. The model also permits an analysis of structural differences in efficiency between West and East German distribution utilities.¹⁸ In fact, the association agreement includes a structural variable ‘East-West’, implying that East German utilities have

on average higher costs than their West German counterparts. This is supposedly due to the structural legacy inherited from socialist times, as well as to the drop in electricity consumption in East Germany after reunification, whereas network sizes have remained constant. In order to test the East-West hypothesis, the sample is split up into 259 West German utilities and 48 East German ones. The results of the East-West comparison are somewhat surprising: East German utilities feature an average efficiency of 77%, against a West German average of 65%.

This result may suggest that investment efforts of the last decade have led to an accelerated modernization process in East Germany, and thus a more efficient use of resources. Electricity production and distribution can now revert to a modernized power station park distribution system. The results tend in the same direction as those of Frontier Economics and Consentec (2003, p. 19), which find that some East German utilities have some of the highest efficiency scores.

¹⁸ The analysis cannot incorporate a ‘modernization’ measure. This is due to the fact that because of limited data availability a static model is applied. Only with panel data one would be able to provide measures of technical change by means of dynamic DEA and SFA models.

Results from the extended model

The study now estimates the efficiency taking into account a broader set of variables. In order to keep the results comparable, the base model is estimated with the reduced data sample of 195 utilities ('Model 2b').

Peak load, turnover and quality. In addition to the traditional inputs, grid line and labour, the study considers peak load (as a proxy for transformer capacity, for which no data are available) to be a separate cost factor. Model 3 thus contains three input and three output variables. The efficiency estimates are slightly higher than before, averaging 73%. No structural correlation is found between the size of a utility and its peak load as a structural variable affecting efficiency. In the case of lacking cost data, it may therefore make sense to work with two different variables accounting for capital costs.

Model 4 introduces a monetary variable, turnover, as output measure. The results are not significantly different from those obtained with Model 2: the average efficiency decreases by about 1 percentage point. This is due only to the drop of the average efficiency of the 50% largest distribution utilities. The average of the smallest one remains the same. An explanation of this uneven effect of the turnover variable could be that larger utilities generally have more industrial customers in relation to household customers. Since industrial customers obtain lower prices and thus lead to a lower average per unit revenue, this has an adverse effect on the efficiency score.

Model 5 attempts to identify the relation between quality and efficiency. The quality of distribution is defined by the electricity losses that occur during this process. As could be expected, the average efficiency of all utilities increases when this additional input is introduced. No difference is detected in the relative change of efficiency scores between the large and small utilities. This result contradicts the common view that large utilities are in possession of better grids.

Grid composition and customer structure. A third structural variable that may have an impact on efficiency scores is the composition of the grid, i.e. the relation of aerial lines to cable lines. The idea behind this reasoning is that cable lines are on average more expensive than aerial lines. However, regional utilities are often not free to choose the most appropriate grid type. This is particularly true in densely settled areas where national law prohibits

aerial lines. The issue is approached in the following way: to show the real cost structure of the capital input the simple grid size variable of the basic model is substituted in Model 6 by a weighted sum of cable and aerial grid. Since cable lines are on average more expensive an upwards factor of 1.25 for each km of cable line is defined, and thereby indirectly higher prices are considered for cables. This takes into account the disadvantage of the utilities that are forced to maintain a high proportion of cable lines.

The first noticeable result is that average efficiency remains almost unchanged; it increases slightly to 67.0% compared with the 66% in the original specification (Model 2b). The modest change in efficiency is not surprising: some utilities use a grid with a higher proportion of cable lines, others with more aerial lines. These two tendencies compensate each other while the average productivity remains almost the same. The efficiency of single utilities, in contrast, changes more significantly: utilities with a higher share of cables benefit from this transformation. All in all, the grid composition does not add much to the interpretation of results, a finding also suggested by Frontier Economics and Consentec (2003, p. vii) who doubt that grid composition is a significant cost driver.

In addition, we now consider the structure of customers. We distinguish between industrial and households customers taking into account the difference in the price structure of the end user prices. We found that the higher the share of industrial customers to total customers, the lower is the efficiency increase from Model 2b to 7. The same result is already noticed in Model 4: that an increase of the share of industrial customers represents a disadvantage for the utilities in terms of efficiency.

Characteristics of most inefficient utilities. In order to detect some regularities of inefficiency we now give a short summary of technical characteristics for the most inefficient firms. For this purpose the extended Models 2b to 7 are considered and sorted out first the 34 most inefficient firms across all models. In a second step these technical indicators (inputs and outputs) of the less efficient utilities are compared with those of the more efficient ones (see Table 4). Within the 34 most inefficient utilities, only one is located in East Germany, which tends to confirm the result that West German utilities tend to be less efficient when compared to their East German counterparts. Notice that all inefficient utilities have proportionally a higher share of network length with respect to

Table 4. Efficiency differences between large and small utilities

Model DEA	Note	Average	First 50% of utilities	Last 50% of utilities
DEA 1	307	0.63	0.69	0.57
DEA 2	307, Inverse Density Index	0.67	0.70	0.64
DEA 2, VRS	307, Inverse Density Index	0.70	0.73	0.67
DEA 2b	195, Inverse Density Index	0.66	0.67	0.64
DEA 3	195, Peak load	0.73	0.74	0.72
DEA 4	195, Turnover	0.65	0.66	0.64
DEA 5	195, Losses	0.71	0.71	0.71
DEA 6	195, Grid composition	0.67	0.68	0.65
DEA 7	195, Customer structure	0.69	0.71	0.68

Table 5. Correlation analysis between DEA models from Section II (reduced data sample)

	DEA – Model 2b CRS	DEA – Model 3 CRS	DEA – Model 4 CRS	DEA – Model 5 CRS	DEA – Model 6 CRS	DEA – Model 7 CRS
DEA – Model 2b CRS	1.00	0.93	0.90	0.90	1.00	0.98
DEA – Model 3 CRS		1.00	0.82	0.86	0.93	0.93
DEA – Model 4 CRS			1.00	0.79	0.90	0.89
DEA – Model 5 CRS				1.00	0.90	0.88
DEA – Model 6 CRS					1.00	0.97
DEA – Model 7 CRS						1.00

their number of customers.¹⁹ A second step checks if there are any regularities between inefficiency and the amount of electricity sold for each customer. Relative to the firm size, there seems to be no such correlation. Further it is noted that inefficiency is related to the electricity sold per employee. Most of the inefficient firms provide a relative low share of electricity sold and employees. Across all firms one finds low revenue per km network length and a share of network length per MWh electricity sold.

Correlation analysis of DEA models. This section again checks the robustness of the results by conducting a correlation analysis for the respective model specifications. Table 5 shows the correlation analysis for Models 2b to 7. Overall, the correlation among the models is high. All are above 79%. Thus one can conclude that the obtained DEA efficiency measures can generally be assumed to be robust.

V. Conclusions

This study has extended the literature on efficiency analysis to the electricity distribution sector in

Germany. In addition to conventional DEA analysis, SFA distance function estimations have been performed, and relatively high correlations found between the two methods. The general issue of optimal utility size and specific issues related to the 'Balkanization', i.e. the atomization of the German electricity distribution industry have been addressed. The results suggest that returns to scale play only a minor role: only very small utilities have a significant cost disadvantage. Low customer density is found to affect the efficiency score significantly in the lower third of the sample. The grid composition does not produce systematic effects. Surprisingly, East German utilities show a higher average efficiency than their West German counterparts. Peak load as a structural input variable does not seem to be an important determinant of efficiency, when compared with the base model without peak load. Utilities with a high share of industrial customers seem to suffer a disadvantage by the efficiency analysis.

Further research should focus on using cost data for the inputs to make comparison of allocative efficiency possible. Additional analysis of quality and its relation with efficiency seems to be the most urgent policy relevant question, but it would require a substantial effort in data collection and treatment.

¹⁹ The ratio of network length and number of customers varies around 0.6. The more efficient firms show a significantly lower ratio. Only some very small more efficient utilities have a higher quotient. But this is due to the fact that they can compensate the high utilization of the input factor capital with a very low utilization of labour.

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